Spatial coherence control of xuv supercontinuum generation by two-color laser field

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Abstract: We investigate the spatial characteristics of xuv supercontinuum generation in the two-color laser field consisting of a fundamental and a weak second harmonic field. By optimizing the synthesized two-color field, the spatial profile of the xuv supercontinuum varies from annular-like to Gaussian-like and then the spatial quality is improved effectively, which is beneficial for its potential applications. Moreover, our calculation shows that the spatial quality of the supercontinuum is stable when the intensity of the controlling field varies in the acceptable fluctuation.

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References and links
It is still challenging to further broaden and enhance supercontinuum. Compressed, and the applications of the attosecond pulse are limited due to the low output energy. However, the duration of the driving pulse can hardly be further compressed, and the applications of the attosecond pulse are limited due to the low output energy. Many efforts have been paid to produce isolated attosecond pulses is using a few-cycle laser pulse, and 10-eV supercontinuum has employed an extremely short laser pulse of 3.3fs to produce a 40-eV supercontinuum [10]. However, the duration of the driving pulse can hardly be further compressed, and the applications of the attosecond pulse are limited due to the low output energy. It is still challenging to further broaden and enhance supercontinuum.

The process of HHG is well understood with the three-step model [11], which shows that the ionization, acceleration and recombination of the electrons determine the time-frequency characteristics of the harmonic generation. The three steps of HHG process can be controlled.
to generate a broadband supercontinuum. It has been proposed that the attosecond pulse bandwidth can be effectively broadened in the polarization-gate scheme [12,13], which can control the recombination of the electrons in the laser field. The two-color field scheme is a promising way to produce the broadband supercontinuum by controlling the electron acceleration (acceleration gating, AG) and ionization (ionization gating, IG) processes [14,15]. Lan et al [15] found that the broadband supercontinuum in the AG scheme can be generated in the cutoff, while the IG scheme produces the supercontinuous high harmonics in the plateau and the harmonic and attosecond pulse yields are higher.

Recent studies mainly focus on the spectral and temporal characteristics of HHG for the goal of the generation of high-efficiency attosecond pulse [10-16], but its spatial characteristics have seldom been investigated. The studies on the spatial characteristics of HHG in the monochromatic field have been reported in the previous works [17-22]. Salières [19] et al. found that the spatial profile of the harmonic in the cutoff region is almost Gaussian in experiment using one-color laser pulse. Moreover, the same group demonstrated that the spatial properties can be controlled and optimized by moving the laser focus position relative to the nonlinear medium [20]. Recently, Tosa et al. [21] pointed out that the chirp of laser field can change the spatial distribution of high-order harmonic generation. Temporal and spatial modifications of the laser pulse can influence the harmonic field both in spectral and spatial characteristics [21]. In the two-color scheme, the laser beam is modified by temporal distribution of the controlling field, and then broadband supercontinuum can be generated effectively. The spatial quality optimization of the supercontinuum is the important issue in many applications, which has been seldom investigated. In this paper, we investigate that spatial characteristics of xuv supercontinuum generation in the \( \omega + 2\omega \) laser field. By optimizing the synthesized two-color field, the spatial profile of the xuv supercontinuum varies from annular-like to Gaussian-like, which implies that the spatial quality can be controlled and improved effectively. Moreover, our calculation shows that the spatial quality of the supercontinuum is stable when the intensity of the controlling field varies in the acceptable fluctuation.

2. Theoretical model

The theoretical description of HHG takes into account both the single-atom response (SAR) to the laser pulse and the collective response of macroscopic gas to the laser and high harmonic fields. In our simulation, SAR is calculated with Lewenstein model [23] and the nonlinear dipole momentum is [in atomic units (a.u.)]

\[
d_{\mu\nu}(t) = i \int_{-\infty}^{t} dt' \left[ \frac{\pi}{\epsilon + i(t-t')/2} \right]^{3/2} \times d^* \left[ p_{\mu\nu}(t',t) - A(t) \right] d \left[ p_{\mu\nu}(t',t) - A(t') \right] \\
\times \exp \left[ -i S_{\mu\nu}(t',t) \right] E(t')g(t') + c.c.,
\]

In the Eq. \( E(t) \) is the electric field, \( A(t) \) is the vector potential. \( \epsilon \) is a positive regularization constant. \( p_{\mu\nu} \) and \( S_{\mu\nu} \) are the stationary momentum and quasiclassical action, which are given by

\[
p_{\mu\nu}(t',t) = \frac{1}{t-t'} \int_{t'}^{t} A(t'') dt'',
\]

\[
S_{\mu\nu}(t',t) = (t-t')I_p - \frac{1}{2} p_{\mu\nu}^2(t',t)(t-t') + \frac{1}{2} \int_{t'}^{t} A^2(t'') dt'',
\]
where $I_p$ is the ionization energy of the helium. $d(p)$ is the dipole matrix element for transitions from the ground state to the continuum state. For hydrogenlike atoms, it can be written as

$$d(p) = i \frac{2^{7/2}}{\pi} \frac{\sqrt{2} p}{(2I_p)^{5/4}} \frac{\exp\left(-\frac{4we}{\omega_h}\right)}{(p^2 + 2I_p)^{3/2}}. \quad (4)$$

$g(t)$ in the Eq. (1) represents the ground state amplitude:

$$g(t') = E_f(t') \exp\left(-\int_{-\infty}^{t'} \omega(t') dt'\right). \quad (5)$$

$\omega(t')$ is the ionization rate, which is calculated by Ammosov-Delone-Krainov (ADK) tunnelling model [24]:

$$\omega(t) = w_e |C_{n'}|^2 \left(\frac{4we}{\omega_h}\right)^{2n'-1} \exp\left(-\frac{4we}{3\omega_h}\right), \quad (6)$$

$$d(p) = i \frac{2^{7/2}}{\pi} \frac{\sqrt{2} p}{(2I_p)^{5/4}} \frac{\exp\left(-\frac{4we}{\omega_h}\right)}{(p^2 + 2I_p)^{3/2}}. \quad (7)$$

$$w_e = \frac{I_p}{h}, \quad \omega_h = \frac{|E_f(t)|}{\sqrt{2m_e}p}, \quad n' = Z \left(\frac{I_{ph}}{I_p}\right)^{1/2}, \quad |C_{n'}|^2 = \frac{2\omega_e}{n'\Gamma(n' + 1)\Gamma(n')} \quad (8)$$

where $Z$ is the net resulting charge of the atom, $I_{ph}$ is the ionization potential of the hydrogen atom, and $e$ and $m_e$ are electron charge and mass respectively.

To simulate the collective response of macroscopic gas, we solve the light propagation for the laser and high harmonic fields in cylindrical coordinate separately [25],

$$\nabla^2 E_l(r,z,t) - \frac{1}{c^2} \frac{\partial^2 E_l(r,z,t)}{\partial t^2} = \frac{\omega_p(r,z,t)^2}{c^2} E_l(r,z,t), \quad (9)$$

$$\nabla^2 E_h(r,z,t) - \frac{1}{c^2} \frac{\partial^2 E_h(r,z,t)}{\partial t^2} = \frac{\omega_p(r,z,t)^2}{c^2} E_h(r,z,t) + \mu_0 \frac{\partial^2 P_{nl}(r,z,t)}{\partial t^2}, \quad (10)$$

where $E_l$ and $E_h$ are the laser field and high harmonics, respectively. $\omega_p$ is the plasma frequency and is given by

$$\omega_p = \sqrt{\frac{n_e(r,z,t)}{m_e \epsilon_0}} \quad (11)$$

The nonlinear polarization of gas is $P_{nl} = n_0d_{nl}$. $n_0$ and $n_e$ are the densities of neutral atoms and free electrons. The electron density can be expressed as

$$n_e(t) = n_0[1 - \exp(-\int_{-\infty}^{t} \omega(t') dt')], \quad (12)$$

3. Result and discussion

In this work, the two-color field is synthesized by a 5-fs linearly polarized driving pulse with a wavelength of 800 nm and a 5-fs linearly polarized control pulse with a wavelength of 400 nm. The peak intensities of the driving and control pulses are $6 \times 10^{14} W/cm^2$ and $2.4 \times 10^{15} W/cm^2$, respectively. The electric field of the synthesized laser pulse is expressed by

$$E(t) = E_0 f(t) \cos(\omega_0 t) + E_f(t) \cos[2\omega_0 t + \phi_0], \quad (13)$$
$E_0$ and $E_1$ are the amplitudes of the driving and controlling field. $f(t)$ and $\omega_0$ are the envelope and the frequency. A Gaussian envelope shape is adopted and $\phi_0$ is set as 0.

We first compare the spectral characteristics of HHG in the two-color field with those in one-color field using Lewenstein model [23, 26]. In the two-color field, by mixing a control laser pulse to the fundamental pulse, the synthesized field can be shaped, which results in the different spectral characteristics of HHG from those in one-color case. The electric field of the two-color field (red solid curve) synthesized by the fundamental (green solid curve) and controlling (the blue dashed curve) fields is shown in Fig. 1(a). The ionization probability in the two-color field is represented by the red dashed line. As shown in Fig. 1(a), the controlling field is in the same direction with the fundamental field at the peak P, where the intensity of the synthesized field is enhanced. Thus, the ionization of the electron is enhanced at P. Further, HHG is also confined within this half-cycle optical cycle. This scheme is named the ionization gate (IG). The harmonic spectrum in the two-color field is presented by the red solid curve in Fig. 1(b). For comparison, the spectrum of HHG in the fundamental field alone is also presented (the green solid curve). As shown in Fig. 1(b), the spectral structure in one-color field is irregular for the harmonics in the plateau and becomes continuous for the harmonics in the cutoff. However, the overall spectrum in the two-color field becomes smooth and regularly modulated for the harmonics through the plateau to cutoff. What’s more, the efficiency of the HHG in the plateau is enhanced by about one order. Our calculation shows that the broadband supercontinuum in the two-color field is generated in the plateau and the yield of the harmonics is higher than that in the one-color field.

![Fig. 1. (a), The electric field of the two-color field (red solid curve) synthesized by the fundamental (green solid curve) and controlling (the blue dashed curve) fields, the ionization probability in the two-color field is presented by the red dashed line. (b), The harmonic spectrum in the two-color field (the red solid curve) and in the fundamental filed alone (the green solid curve)](image)

Next, we investigate the spatial characteristics of the efficient broadband supercontinuum described above. For convenience, the harmonics from 40th-60th in the plateau are taken as our
Fig. 2. The near-field spatial profiles of 40th-60th harmonics at the exit of the medium in the one-color field (a) and the two-color field (b), and the corresponding spatial images of the harmonics are also presented in (c) and (d).

object of study. In the nonadiabatic three-dimensional propagation simulations [25], we utilize a 0.45-mm long gas target with a density of $1.37 \times 10^{18}$ cm$^{-3}$, which corresponds to a gas pressure of 40 Torr at room temperature. The focuses of the fundamental field and controlling field are put at the same position and the beam waists are both 25 $\mu$m. The entrance of the gas jet is placed 2 mm after the focuses of the laser field. Other parameters are the same as in Fig. 1. The near-field spatial profiles of 40th-60th harmonics at the exit of the medium in the one-color and the two-color fields are shown in Fig. 2, and the corresponding spatial images of the harmonics are also represented in Figs. 2(c) and (d). In the one-color field in Figs. 2(a) and (c), the near-field spatial profile of 40th-60th harmonics in the fundamental field alone is Gaussian-like. It is believed that the spatial quality of HHG with a Gaussian profile is better than that with an annular-like profile, and then the high-order harmonics in the one-color field has a good spatial quality. As we known, the spatial distribution of the laser field and phase matching of HHG in macroscopic medium play an important role in the spatial profile of HHG. When the laser focus is put before the gas target, short trajectory is preferably selected in the propagation and better phase matching of the short trajectory contribution to harmonics in the plateau is obtained off-axis [27]. However, the incident one-color field is Gaussian in space, which results in Gaussian distribution of high-order harmonic generation. Figure 2(b) shows the near-field spatial profile of HHG in the two-color field. Compared with those in one-color case, the near-field spatial profile of HHG in the two-color case is an annular-like distribution, which implies that the spatial quality of the supercontinuum in the two-color case is poor.

The poor spatial quality of the supercontinuum in the two-color field limits its potential applications. We propose an efficient method to control and improve the spatial quality of the broadband supercontinuum by optimizing the synthesized field. Figure 3 shows the near-field spatial images and profiles of HHG in the two-color field with different focus positions and beam waists of the controlling field. In Figs. 3(a) and (e), the parameters are the same as those in Fig. 2(b), and the spatial profile of the HHG is annular-like. The spatial quality is not improved when the beam waist and focus position of the controlling field are 25 $\mu$m and 0 mm (seen in Figs. 3(b) and (f)). However, when the beam waist of the controlling field is further decreased to 20 $\mu$m and the corresponding focus position is 0 mm (seen in Figs. 3(c) and (g)), the spatial profile of the HHG becomes a similar rectangle. When the beam waist of the controlling field
Fig. 3. The near-field spatial images and profiles of HHG in the two-color field with different beam waists and focus positions of the controlling field. The beam waist and focus position are set as 25μm and 2mm (a and e), 25μm and 0mm (b and f), 20μm and 0mm (c and g), 15μm and 0mm (d and h), respectively. The other parameters are same in Fig. 2(b).

...is reduced to 15μm and the focus position is 0mm (seen in Figs. 3(d) and (h)), the harmonic profile becomes nearly Gaussian, which implies that the spatial quality of the supercontinuum has been optimized. Figure 3 shows that the spatial quality of the broadband supercontinuum in the two-color field can be effectively controlled and optimized.

Figure 4(b) shows the far-field spatial profiles of the supercontinuum[28]. For comparison, the near-field spatial profiles in Figs. 3(e) and (h) are represented by the red dashed and blue curve in Fig. 4(a), respectively. The near-field spatial profile represented by the red dashed in Fig. 4(a) is annular-like, and the corresponding far-field spatial quality in Fig. 4(b) is a little improved, which is rectangle-like. When the near-field spatial profile represented by the blue curve is Gaussian-like, the far-field spatial profile is also the Gaussian-like and the divergence angle is smaller than that of the similar rectangle profile.

The spatial distribution of the two-color field influences critically the spatial profile of the harmonic generation. Figure 4 shows the integral of the two-color field at the ionization times of the trajectories corresponding to the 40th-60th harmonics in the plateau. The parameters in Figs. 5(a) and (b) are the same as those in Figs. 3(a) and (d), respectively. For the single-atom response, when the intensity of the laser pulse is much lower than the saturation intensity of the model atom, the harmonic efficiency is mainly determined by the ionization rate. As shown in Fig. 3(a), the laser field off the propagation axes is more intense than that on the axes, which results in higher ionization rate off the propagation axes. Thus, brighter harmonic field can be generated off the axes. However, when the beam waist of the controlling field is 15μm and the focus position is 0mm (seen in Fig. 5(b)), the laser field on the propagation axes is more intense than that off the axes, thus the harmonics on the axes (seen in Fig. 3(d)) is brighter than that off the axes. It is shown that the integral maps of the two-color field at the ionization times of the trajectories corresponding to the 40th-60th harmonics are consistent with the spatial distribution of HHG.

Last, we investigate the influence of the focus position and intensity of the controlling field on the spatial characteristics of the broadband supercontinuum. In Fig. 6(a), the focus position of the controlling field is changed and other parameters are the same as those in Fig. 3(d). When the focus position of the controlling field is 2mm, the spatial profile of HHG is annular-like,
Fig. 4. The near-field (a) and the corresponding far-field (b) profiles of HHG: The beam waist and focus position of the controlling field are set as 25µm and 2mm (the red dashed), 15µm and 0mm (the red curve).

Fig. 5. The integral of the laser field at the ionization times of the trajectories corresponding to the 40th-60th harmonics in the plateau. The parameters in Figs. 4(a) and (b) are the same as those in Figs. 3(a) and (d), respectively.
which implies that the intensity of HHG off the axes is more intense than that on the axes. As the focus position is set as 1mm or 0mm, the spatial profile of HHG becomes Gaussian-like. Figure 6(b) shows that the spatial profiles of HHG in the two-color field with different intensities of the controlling field. Other parameters are the same as those in Fig. 3(d). As shown in Fig. 6(b), the spatial profiles of HHG for the different intensities $I_2$ of the controlling field are all the Gaussian-like shape. When the intensity of the controlling is increased from $2.4 \times 10^{13}$ W/cm$^2$ to $5.4 \times 10^{13}$ W/cm$^2$, i.e. the relative intensity varies from 0.04 to 0.09, the divergence angle of HHG becomes smaller. From Fig. 6, it is shown that the spatial profile of the supercontinuum is stability to the intensity variation of the controlling field and sensitivity to the focus position.

4. Conclusion

In conclusion, we have investigated the spectral and spatial characteristics of xuv supercontinuum generation in the $\omega + 2\omega$ laser field. It is shown that HHG can be confined within half optical cycle in the two-color field and then high-efficiency supercontinuum is generated in the plateau, while the spatial profile of the supercontinuum is an annular-like distribution, which limits its application. By optimizing the two-color filed, the spatial profile of the xuv supercontinuum varies from annular-like to Gaussian-like, which shows that the spatial quality of the supercontinuum in the two-color field can be controlled and optimized effectively. Moreover, when the relative intensity the controlling field varies from 0.04 to 0.09, the spatial profile of the supercontinuum shows stability.

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